

#58 Theorem:

The difference of the squares of any two consecutive integers is odd.

Proof:

Suppose m and n are two arbitrarily chosen consecutive integers k , and $k+1$.

By Substitution,

$$n^2 - m^2 = (k^2 + 2k + 1) - k^2 \quad \text{- Basic Algebra}$$

Let some integer S be equal to the equation

$$S = (k^2 + 2k + 1) - k^2$$

By Basic Algebra:

$$S = 2k + 1$$

- Definition of Odd

Thus, S is odd

QED