

3. (5 pts) Carefully prove: the difference between any two odd integers is even.

Suppose  $m$  and  $n$  are any two odd integers.  
By definition of odd,  $m = 2k+1$  and  $n = 2k'+1$  for some integer  $k$ .

$$m+n = (2k+1) + (2k'+1)$$

$$= 4k+2$$

$$= 2(2k+1)$$

Let  $t = 2k+1$  where  $t$  is an integer  
 $\therefore m+n = 2t$  by definition of even.

4. (5 pts) Carefully prove: the quotient of any two nonzero rational numbers is rational.